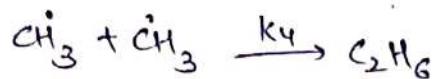
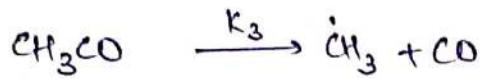
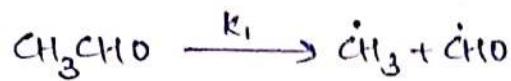


# Assignment - 9 Solutions

1. Pyrolysis of acetaldehyde follows these elementary steps



Expression for decomposition of  $\text{CH}_3\text{CHO}$ :

$$-\frac{d[\text{CH}_3\text{CHO}]}{dt} = k_1[\text{CH}_3\text{CHO}] + k_2[\dot{\text{C}}\text{H}_3][\text{CH}_3\text{CHO}] - \dots \quad (1)$$

We have to calculate concentration of  $\dot{\text{C}}\text{H}_3$  using steady state approximation.

$$\frac{d[\dot{\text{C}}\text{H}_3]}{dt} = k_1[\text{CH}_3\text{CHO}] - k_2[\dot{\text{C}}\text{H}_3][\text{CH}_3\text{CHO}] + k_3[\text{CH}_3\dot{\text{C}}\text{O}] - 2k_4[\dot{\text{C}}\text{H}_3]^2 = 0 \quad (2)$$

We again write expression for calculating  $\text{CH}_3\dot{\text{C}}\text{O}$  intermediate concentration.

$$\frac{d[\text{CH}_3\dot{\text{C}}\text{O}]}{dt} = k_2[\dot{\text{C}}\text{H}_3][\text{CH}_3\text{CHO}] - k_3[\text{CH}_3\dot{\text{C}}\text{O}] = 0 \quad (3)$$

$$\text{From (3)} \quad [\text{CH}_3\dot{\text{C}}\text{O}] = \frac{k_2[\dot{\text{C}}\text{H}_3][\text{CH}_3\text{CHO}]}{k_3} \quad (4)$$

(4) in (2)

$$k_1[\text{CH}_3\text{CHO}] - k_2[\dot{\text{C}}\text{H}_3][\text{CH}_3\text{CHO}] + \frac{k_2 \cdot k_2}{k_3} [\dot{\text{C}}\text{H}_3][\text{CH}_3\text{CHO}] - 2k_4[\dot{\text{C}}\text{H}_3]^2 = 0$$

$$k_1[\text{CH}_3\text{CHO}] = 2k_4[\dot{\text{C}}\text{H}_3]^2$$

$$[\text{CH}_3] = \frac{k_1}{2k_4} \sqrt{[\text{CH}_3\text{CHO}]} - (5)$$

Put (5) in (1)

$$\boxed{-\frac{d[\text{CH}_3\text{CHO}]}{dt} = k_1 [\text{CH}_3\text{CHO}] + \frac{k_2 k_1}{2k_4} [\text{CH}_3\text{CHO}]^2}$$

2. According to Langmuir Adsorption isotherm

(1)

$$\Theta = \frac{KP}{1+KP} - ①$$

Reciprocating above equation

$$\frac{1}{\Theta} = \frac{1}{KP} + 1 - ②$$

Given  $v \rightarrow$  volume of gas adsorbed on surface of solid.

Let  $V \rightarrow$  volume corresponding to total coverage.

$$\therefore \Theta \text{ (fractional coverage)} = \frac{v}{V} - ③$$

Put (3) in (2)

$$\frac{V}{v} = \frac{1}{KP} + 1 - ④$$

We have to plot  $P/v$  graph versus  $P$ ,  $\therefore$  we eliminate from  $V$  by multiplying eq. (4) by  $\frac{P}{V}$  we get LHS

$$\frac{P \times \frac{V}{v}}{V} = \frac{1}{KP} \times \frac{P}{V} + \frac{P}{KV} \Rightarrow \frac{P}{v} = \frac{1}{KV} + \frac{P}{V} - ⑤$$

Thus, eq. (5) is straight line equation, where plot of  $\frac{P}{v}$  versus  $P$  gives straight line, slope  $= \frac{1}{V}$  & intercept  $= \frac{1}{KV}$

(ii) We have to show for small coverages plot of  $\ln\left(\frac{\theta}{P}\right)$  vs  $\theta$  is also a straight line.

$$\text{from eq. (i)} \quad \theta(1+KP) = KP$$

$$\theta + KP\theta = KP$$

$$\theta = KP - KP\theta$$

$$\theta = KP(1 - \theta)$$

$$\frac{\theta}{P} = K(1 - \theta)$$

Taking natural log both sides

$$\ln\left(\frac{\theta}{P}\right) = \ln K + \ln(1 - \theta)$$

If  $\theta \ll 1$ , mathematically  $\ln(1 - \theta) \approx -\theta$  so we get

$$\ln\left(\frac{\theta}{P}\right) = \ln K - \theta$$

So, plot of  $\ln\left(\frac{\theta}{P}\right)$  versus  $\theta$  will also be a straight line with slope = -1 & intercept =  $\ln K$ .

$$3. \quad K = 1.25 \text{ kPa}^{-1}, \theta = 20\% = 0.2$$

Surface coverage ( $\theta$ ) is given as

$$\theta = \frac{KP}{1+KP}$$

Solving above equation for pressure

$$\theta(1+KP) = KP$$

$$P = \frac{\theta}{K(1-\theta)} = \frac{0.2}{1.25 \times 10^3 \text{ Pa}^{-1} (1-0.2)}$$

$$P = 2 \times 10^{-4} \text{ Pa}$$

4.  $V_{\text{mono}} = 130 \text{ cm}^3$  (monolayer volume)

$22.4 \text{ L}$  of any gas = 1 mol of its molecules

$$\therefore \text{no. of molecules present in } V_{\text{mono}} = \frac{6.022 \times 10^{23} \text{ mol}^{-1} \times 130 \times 10^{-3} \text{ dm}^3}{22.4 \text{ dm}^3 \text{ mol}^{-1}}$$

$$= 3.49 \times 10^{21}$$

$$\begin{aligned}\text{Area of cross-section of one molecule} &= 0.162 \text{ nm}^2 \\ &= 0.162 \times 10^{-18} \text{ m}^2\end{aligned}$$

$$\therefore \text{area covered by } 3.49 \times 10^{21} \text{ molecules} = 0.162 \times 10^{-18} \text{ m}^2 \times 3.49 \times 10^{21}$$

$$= 565.38 \text{ m}^2$$

5. (1) Adsorption of  $\text{O}_3$  without dissociation



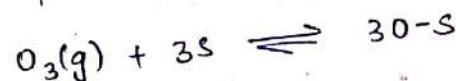
$$\theta = \frac{b P_{\text{O}_3}}{1 + b P_{\text{O}_3}}$$

(2) Adsorption via dissociation into  $\text{O}_2$  &  $\text{O}$



$$\theta = \frac{(b P_{\text{O}_3})^{\frac{1}{2}}}{1 + (b P_{\text{O}_3})^{\frac{1}{2}}}$$

(3) Adsorption via dissociation into  $\text{O}$  &  $\text{O}^+$



$$\theta = \frac{(b P_{\text{O}_3})^{\frac{1}{3}}}{1 + (b P_{\text{O}_3})^{\frac{1}{3}}}$$

## 5

### 6. Langmuir adsorption isotherm:

$$\Theta = \frac{KP}{1+KP} \quad \text{--- (1)}$$

mass adsorbed,  $m_1 = 0.63 \text{ mg}$  at  $P_1 = 36.0 \text{ kPa}$

$m_2 = 0.21 \text{ mg}$  at  $P_2 = 4.0 \text{ kPa}$

We have to calculate fractional coverage  $\Theta_1 + \Theta_2$  at  $P_1 + P_2$

$$\Theta = \frac{\text{madsorbed}}{m_{\text{mono}}} , \text{ from (1)} \quad K = \frac{\Theta}{P(1-\Theta)}$$

Setting expression for  $K$  at one pressure =  $K$  at 2nd pressure

$$\frac{\Theta_1}{P_1(1-\Theta_1)} = \frac{\Theta_2}{P_2(1-\Theta_2)}$$

$$\frac{\frac{m_1}{m_{\text{mono}}}}{P_1 \left(1 - \frac{m_1}{m_{\text{mono}}}\right)} = \frac{\frac{m_2}{m_{\text{mono}}}}{P_2 \left(1 - \frac{m_2}{m_{\text{mono}}}\right)}$$

$$\text{So, } \frac{P_1(m_{\text{mono}} - m_1)}{m_1} = \frac{P_2(m_{\text{mono}} - m_2)}{m_2}$$

$$(m_{\text{mono}} P_1 - P_1 m_1) m_2 = m_1 (P_2 m_{\text{mono}} - P_2 m_2)$$

$$m_{\text{mono}} = \frac{P_1 - P_2}{\frac{P_1}{m_1} - \frac{P_2}{m_2}} = \frac{(36 - 4) \text{ kPa}}{\left(\frac{36}{0.63} - \frac{4}{0.21}\right) \text{ kPa mg}^{-1}}$$

$$= 0.84 \text{ mg}$$

$$\Theta_1 = \frac{0.63}{0.84} = 0.75$$

$$\text{& } \Theta_2 = \frac{0.21}{0.84} = 0.25$$